

Reg. No. : .....

Name : .....

Third Semester B.Tech. Degree Examination, January 2015  
(2008 Scheme)

08.301 : ENGINEERING MATHEMATICS – II (CMPUNERFTAHS)

Time : 3 Hours

Max. Marks : 100

PART – A

Answer **all** questions. **Each** question carries **4** marks.



1. Evaluate  $\int_0^4 \int_0^{x^2} e^{y/x} dy dx$ .

2. Find the area in the first quadrant bounded by the x-axis and the curves  $x^2 + y^2 = 10$ ,  $y^2 = 9x$ .

3. Find the workdone by the force  $\vec{F} = x\hat{i} + 2y\hat{j}$  when it moves a particle on the curve  $2y = x^2$  from  $(0, 0)$  to  $(2, 2)$ .

4. Find the half range sine series of  $f(x) = x$  in  $(0, 2)$ .

5. Expand  $f(x) = x^2$ ,  $-\pi < x < \pi$  in a Fourier series.

6. Obtain the Fourier sine transform of  $\frac{1}{x}$ .

7. Find the p.d.e. of all spheres whose centres lie on the z-axis.

8. Solve  $xp - y^2q^2 = 1$ .

9. Find the particular integral of  $\nabla^2 u = -xy$ .

10. If the solution of one-dimensional heat flow equation depends on Fourier cosine series, what would have been the nature of the end conditions.

P.T.O.



## PART - B

Answer **one** question from **each** Module. **Each** question carries **20** marks.

## Module - I

11. a) Change the order of integration in the integral  $I = \int_0^a \int_{x^2/a}^{2a-x} xy \, dy \, dx$  and evaluate it.

b) Find the volume enclosed by the paraboloid  $x^2 + y^2 = 4z$  and  $z = 4$ .

c) Verify Green's theorem in a plane with respect to  $\int_C (x^2 dx - xy dy)$  where C is the boundary of the square formed by  $x = 0$ ,  $y = 0$ ,  $x = a$ ,  $y = a$ .

12. a) Evaluate  $\iint (x^2 + y^2) \, dx \, dy$  throughout the area enclosed by the curves  $y = 4x$ ,  $x + y = 3$ ,  $y = 0$  and  $y = 2$ .

b) Evaluate  $\oint (e^x dx + 2y dy - dz)$  where C is the curve  $x^2 + y^2 = 4$ ,  $z = 2$ .

c) Using divergence theorem show that  $\int_S \nabla r^2 \cdot d\vec{s} = 6V$ , where S is any closed surface enclosing a volume V.

## Module - II

13. a) Find the Fourier series of  $f(x) = x + x^2$ ,  $-\pi < x < \pi$ . Given that  $f(x)$  is periodic with period  $2\pi$  using the series deduce that

$$\text{i) } \frac{\pi^2}{12} = 1 - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$$

$$\text{ii) } \frac{\pi^2}{6} = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots$$

b) Obtain the Fourier cosine transform of  $f(x) = \sin x$  in  $0 < x < \pi$ .

c) What are Dirichlet's conditions for a Fourier series ?



14. a) Show that  $e^{\frac{-x^2}{2}}$  is self reciprocal.
- b) Prove that  $F[x^n f(x)] = (-i)^n \frac{d^n}{ds^n} F(s)$ .
- c) Write the Fourier sine series of  $K$  in  $(0, \pi)$ .

**Module – III**



15. a) Solve  $\left(\frac{y-z}{yz}\right)p + \frac{z-x}{zx}q = \frac{x-y}{xy}$ .

b) Solve  $p^2x^2 + q^2y^2 = z^2$ .

c) A string of length 'l' is fastened at both ends. The midpoint of the string is taken to a height 'b' and then released from rest in that position. Find the displacement of the string.

16. a) Derive one-dimensional heat equation.

b) A bar 10 cm long with insulated sides has its ends A and B maintained at temperatures 50°C and 100°C respectively until steady-state conditions prevail. The temperatures at A is suddenly raised to 90°C and at the same time that at B is lowered to 60°C. Find the temperature distribution in the bar at time t.

c) Solve  $(D^2 + D'^2)z = e^{x+2y}$ .

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